Derivatives of Exponential and Logarithm Functions

Differentiate each of the following functions.

$$\mathbf{1.} \ Q(w) = \frac{\ln(w)}{2w^5}$$

2.
$$g(z) = 12 \ln(z) - 5z^3 e^z$$

Inverse Trig Functions

Differentiate each of the following function.

3.
$$f(y) = \tan^{-1}(y) + y^2 \sin^{-1}(y)$$

4.
$$y = \cos(x)\cos^{-1}(x)$$

Chain Rule

For problems 5-9 differentiate the given function.

5.
$$U(t) = 6\sec^4(t) - \csc(7t)$$

6.
$$g(x) = \sqrt{7+3x} \cos(2-x)$$

7.
$$y = \frac{e^{3t}}{6t - \sin(4t)}$$

8.
$$h(y) = \left[\sqrt{11y} + \ln(3y - \tan(y))\right]^4$$

9.
$$f(x) = \cot^5 (7x + e^{\sin(5x)})$$

10. Determine where $y = \ln(2w^4 - w^3 - 3w^2 + 25)$ is not changing.

11. Determine where in [-20, 40] the function $f(x) = 6x + 12\sin(\frac{x}{3})$ is increasing and decreasing?

12. Determine where $h(t) = -2t^2 e^{4-t^2}$ is increasing and decreasing.